

Tailoring graphene electronic properties *via* adsorption of hydrogen atoms

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Outline

- 1 Introduction
 - General
 - Basics
- 2 H atoms on graphenic substrates
 - Single atom adsorption
 - Clusters of H atoms
 - The role of edges
- 3 Opening a bandgap
 - H superlattices



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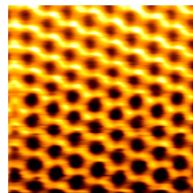
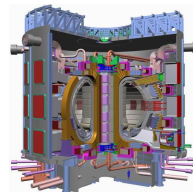
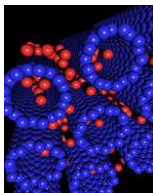
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Technology

- Hydrogen storage
- Nuclear fusion
- Nanoelectronics, spintronics, nanomagnetism



Technology

Electric Field Effect in Atomically Thin Carbon Films

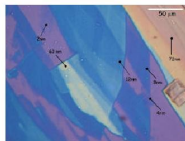
K. S. Novoselov,¹ A. K. Geim,^{1*} S. V. Morozov,² D. Jiang,¹
Y. Zhang,¹ S. V. Dubonos,² I. V. Grigorieva,¹ A. A. Firsov²

We describe monocrystalline graphitic films, which are a few atoms thick but are nonetheless stable under ambient conditions, metallic, and of remarkably high quality. The films are found to be a two-dimensional semimetal with a tiny overlap between valence and conduction bands, and they exhibit a strong ambipolar electric field effect such that electrons and holes in concentrations up to 10^{14} per square centimeter and with room-temperature mobilities of $\sim 10,000$ square centimeters per volt-second can be induced by applying gate voltage.

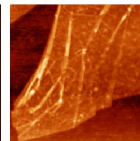
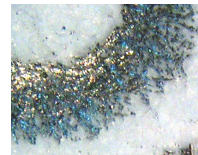
The ability to control electronic properties of a material by externally applied voltage is at the heart of modern electronics. In many cases, it is the electric field effect that allows one to vary the carrier concentration in a semiconductor device and, consequently, change an electric current through it. As the

semiconductor industry is nearing the limits of performance improvements for the current technologies dominated by silicon, there is a constant search for new, nontraditional materials whose properties can be controlled by the electric field. The most notable recent examples of such materials are organic conductors (1) and carbon nanotubes (2). It has long been tempting to extend the use of the field effect to metals [e.g., to develop all-metallic transistors that could be scaled down to much smaller sizes and would consume less energy and operate at higher frequencies

than traditional materials. However, metal film screened by a dielectric and bulk materials tend to be coming down to a few nanometers; so far, this has proved to be an insurmountable obstacle to metallic elec-

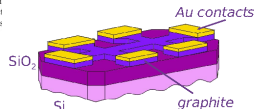


graphene sheets rolled up into nanometer-sized cylinders (3–7). Planar graphene has been presumed not to exist because of its instability with respect to curved structures such as carbon nanotubes (5–14).



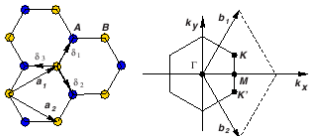
¹Department of Physics, University of Manchester, Manchester M13 9PL, UK. ²Institute for Microelectronics Technology, 142432 Chernogolovka, Russia.

*To whom correspondence should be addressed.
E-mail: geim@man.ac.uk



Technology

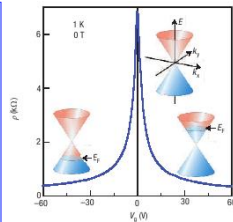
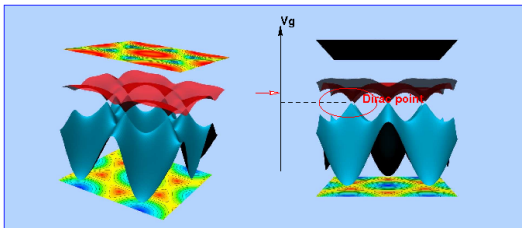
$$H \approx -t \sum_{i,\tau} \sum_j a_{\tau}^{\dagger}(\mathbf{R}_i) b_{\tau}(\mathbf{R}_i + \delta_j) + c.c.$$



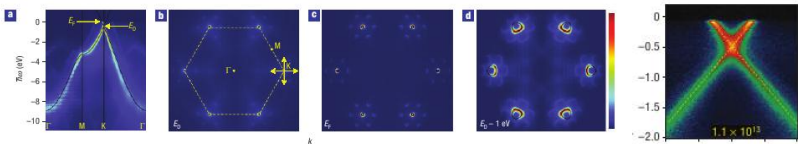
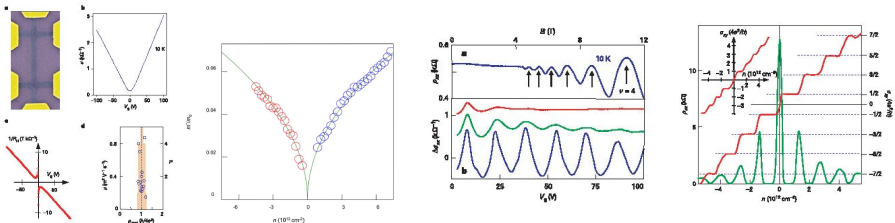
$$a_{\tau,i} = \frac{1}{N} \sum_{\mathbf{k}} e^{-i\mathbf{k}\mathbf{R}_i} a_{\tau}(\mathbf{k})$$

$$H = -t \sum_{\mathbf{k},\tau} f(\mathbf{k}) a_{\tau}^{\dagger}(\mathbf{k}) b_{\tau}(\mathbf{k}) + c.c.$$

$$H = -t \sum_{\mathbf{k},\tau} \begin{bmatrix} a_{\tau}^{\dagger}(\mathbf{k}), b_{\tau}^{\dagger}(\mathbf{k}) \end{bmatrix} \begin{bmatrix} 0 & f(\mathbf{k}) \\ f^*(\mathbf{k}) & 0 \end{bmatrix} \begin{bmatrix} a_{\tau}(\mathbf{k}) \\ b_{\tau}(\mathbf{k}) \end{bmatrix}$$



Technology



Technology

Graphene is a **true 2D-electron gas (2DEG)** system with **pseudo-relativistic** conduction electrons!

...why interesting for us?

- **Chemistry:** graphene is a large polycyclic **aromatic** hydrocarbon
- **Surface Science:** **adsorption** of atoms/molecules may tremendously affect transport properties



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The need for understanding adsorption

H on Graphite (Graphene) vs metal substrates

- Chemisorption is thermally **activated**^{1,2}
- Substantial **lattice reconstruction** upon sticking^{1,2}
- Diffusion of chemisorbed H atoms does **not** occur³
- **Preferential** sticking³
- **Clustering** of H atoms^{3,4,5}
- **Dimer** recombination⁶

[1] L. Jelaica and V. Sidis, *Chem. Phys. Lett.* 300, 157 (1999) [2] X. Sha and B. Jackson, *Surf. Sci.* 496, 318 (2002)
[3] L. Hornekaer *et al.*, *Phys. Rev. Lett.* 97, 186102 (2006) [4] A. Andree *et al.*, *Chem. Phys. Lett.* 425, 99 (2006) [5]
L. Hornekaer *et al.*, *Chem. Phys. Lett.* 446, 237 (2007) [6] L. Hornekaer *et al.*, *Phys. Rev. Lett.* 96, 156104 (2006)

Theoretical tools

I. Tight-binding π Hamiltonian (uncorrelated e^-)

$$H \approx H^{TB} = \sum_{\tau, ij} (t_{ij} a_{i,\tau}^\dagger b_{j,\tau} + t_{ji} b_{j,\tau}^\dagger a_{i,\tau}) + \text{next-to-}nn + \text{etc...}$$

II. Hubbard (partially correlated e^-)

$$H \approx H^{TB} + \sum_i U_i n_{i,\uparrow} n_{i,\downarrow}$$



III. Valence-Bond (partially correlated e^-)

$$\Psi_{VB} = \mathcal{A}\{\phi_1 \phi_2 \phi_3 \dots \phi_N \Theta_{S,M}^N\}$$

IV. DFT calculations ('fully' correlated e^-) and more..

- Periodic, plane-wave based, spin-polarized calculations with **VASP**
- **PAW** method, **PBE** functional
- **5x5x1 unit cell**, $c=20$ Å (vacuum), **6x6x1** Γ -centered k mesh, $E_{cut} = 500$ eV



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I. Properties of *bipartite* lattices

$$H^{TB} = \sum_{\sigma, ij} (t_{ij} a_{i,\sigma}^\dagger b_{j,\sigma} + t_{ji} b_{j,\sigma}^\dagger a_{i,\sigma})$$

Electron-hole symmetry

$$b_i \rightarrow -b_i \implies \mathbf{h} \rightarrow -\mathbf{h}$$

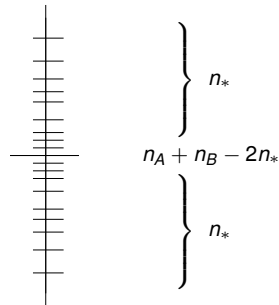
if ϵ_i is eigenvalue and

$$c_i^\dagger = \sum_j \alpha_j a_j^\dagger + \sum_j \beta_j b_j^\dagger \text{ eigenvector}$$



$-\epsilon_i$ is also eigenvalue and

$$c_i'^\dagger = \sum_j \alpha_j a_j^\dagger - \sum_j \beta_j b_j^\dagger \text{ is eigenvector}$$



I. Properties of *bipartite* lattices

$$H^{TB} = \sum_{\tau, ij} (t_{ij} a_{i,\tau}^\dagger b_{j,\tau} + t_{ji} b_{j,\tau}^\dagger a_{i,\tau})$$

Theorem

If $n_A > n_B$ there exist (at least) $n_I = n_A - n_B$ "midgap states" with vanishing components on B sites

Proof.

$$\begin{bmatrix} \mathbf{0} & \mathbf{T}^\dagger \\ \mathbf{T} & \mathbf{0} \end{bmatrix} \begin{bmatrix} \alpha \\ \beta \end{bmatrix} = \begin{bmatrix} \mathbf{0} \\ \mathbf{0} \end{bmatrix} \text{ with } \mathbf{T} \text{ } n_B \times n_A (> n_B)$$

$$\Rightarrow \mathbf{T}\alpha = \mathbf{0} \text{ has } n_A - n_B \text{ solutions}$$



II. Properties of *bipartite* lattices

$$H^{Hb} = \sum_{\tau, ij} (t_{ij} a_{i,\tau}^\dagger b_{j,\tau} + t_{ji} b_{j,\tau}^\dagger a_{i,\tau}) + U \sum_i n_{i,\tau} n_{i,-\tau}$$

Theorem

If $U > 0$, the ground-state at half-filling has

$$S = |n_A - n_B|/2 = n_I/2$$

Proof.

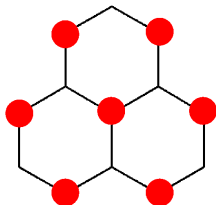
E.H. Lieb, *Phys. Rev. Lett.* **62** (1989) 1201



...basically, we can apply **Hund's rule** to previous result



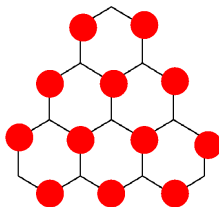
Bipartite lattices: theorems at work



$$n_A = n_B + 1$$

$$S = 1/2$$

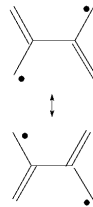
patterned spin-density..



$$n_A = n_B + 2$$

$$S = 1$$

..triplet ground-state

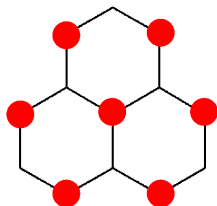


$$n_A = n_B$$

$$S = 0$$

'open-shell singlet'

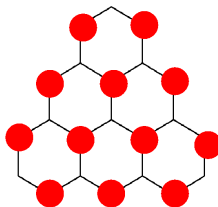
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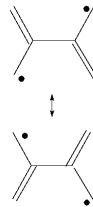
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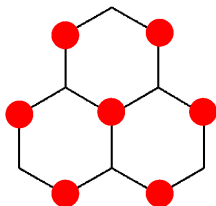


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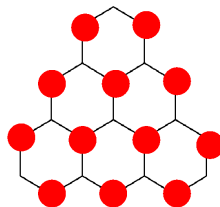
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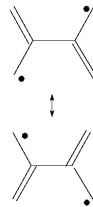
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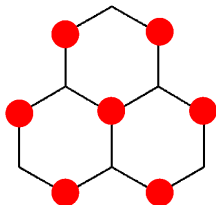


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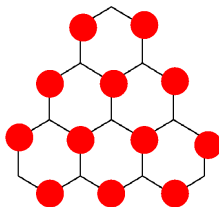
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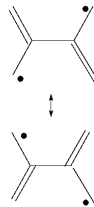
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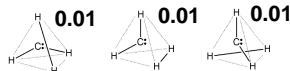
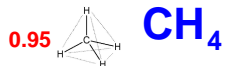
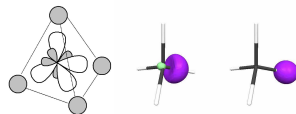
III. Valence Bond picture

Modern, basic VB *ansatz*

$$\Psi = \mathcal{A}\{\phi_1\phi_2\phi_3\ldots\phi_N\Theta_{S,M}^N\}$$

$$\Theta_{S,M}^N = \sum_k^{f_s^N} c_k \Theta_{S,M;k}^N$$

- orbitals ϕ_i are (or turn out to be) **localized on atoms**
- spin-function is the best coupling for the given S



$$\Psi = \sum_{k=1}^{42} c_k \mathcal{A}\{\phi_1 \ldots \phi_{10} \Theta_{0,0;k}^{10}\}$$

$$\sim \mathcal{A}\{\phi_1 \ldots \phi_{10} \Theta^{PP}\}$$



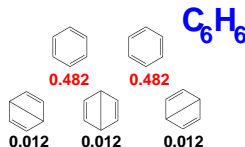
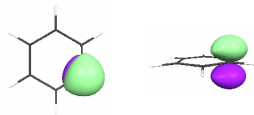
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$$\Psi = \sum_{k=1}^6 c_k \mathcal{A}\{\phi_1\phi_2\phi_3\phi_4\phi_5\phi_6\Theta_{0,0;k}^6\}$$

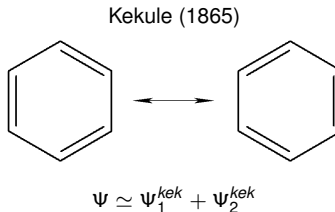
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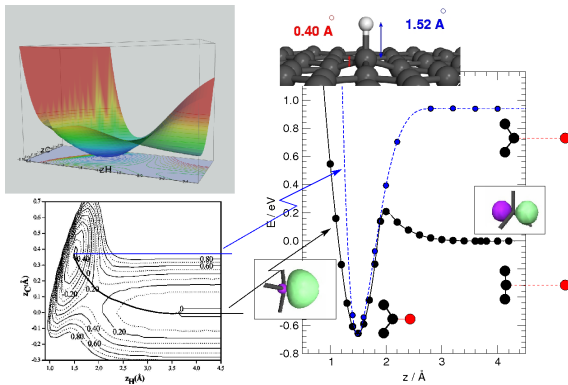
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Adsorption PES

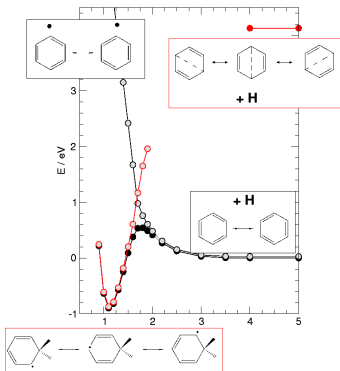
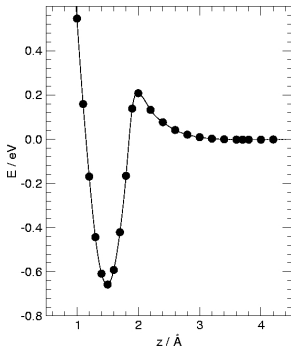


X. Sha and B. Jackson, *Surf. Sci.* 496, 318 (2002)

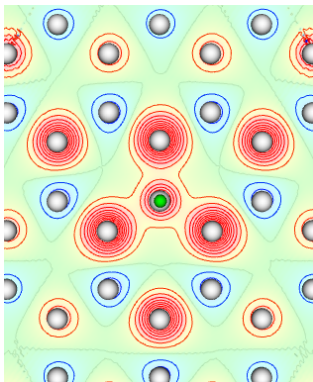


Single H

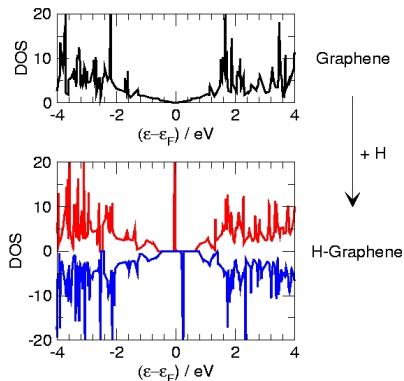
Valence Bond: adsorption barrier



Substrate electronic structure

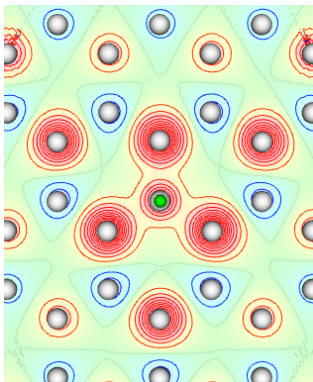


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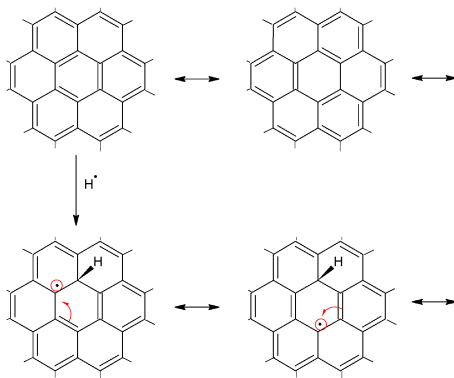


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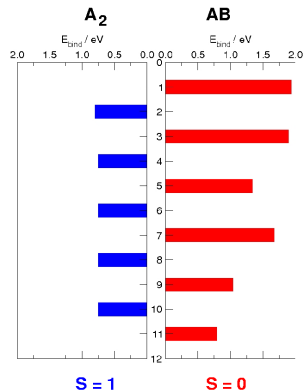
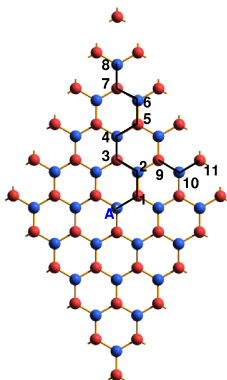


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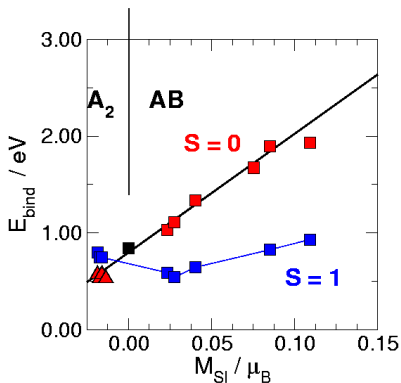


Clustering of H atoms

Dimers



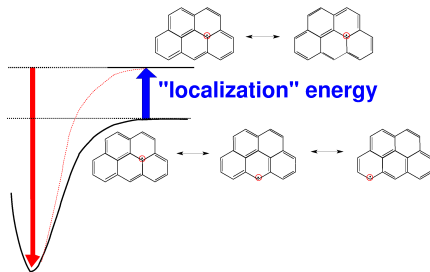
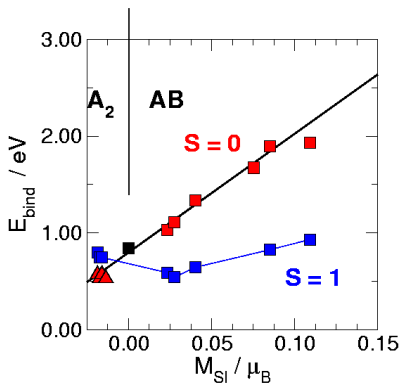
Dimers



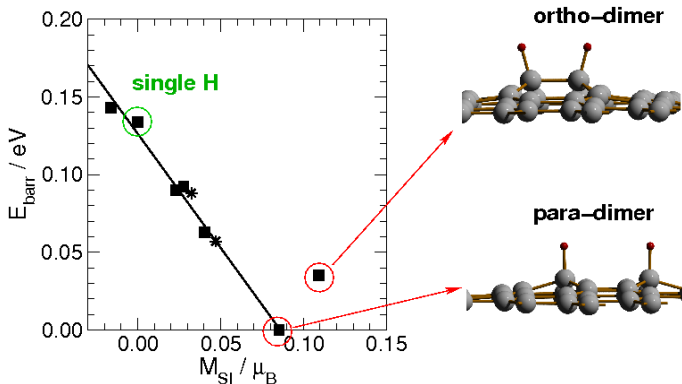
Binding energies depend \sim
linearly on the site integrated
magnetization (M_{SI})



Dimers

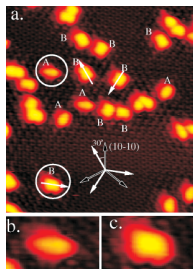


Dimers

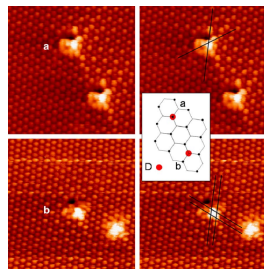
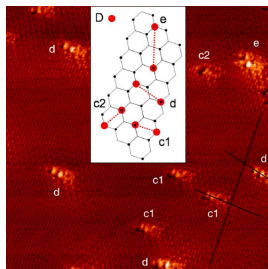


Clustering of H atoms

Dimers



[1]



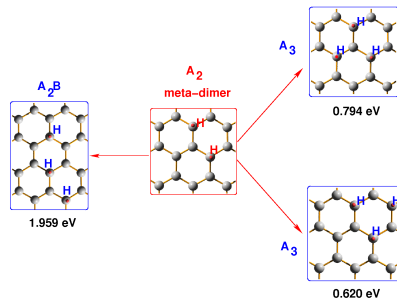
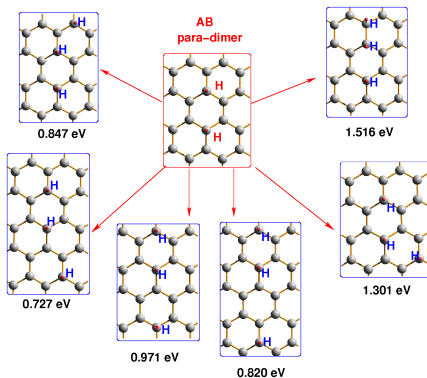
[2]

[1] L. Hornekaer, Z. Sljivancanin, W. Xu, R. Otero, E. Rauls, I. Stensgaard, E. Laegsgaard, B. Hammer and F. Besenbacher. Phys. Rev. Lett. 96 156104 (2006)

[2] A. Andree, M. Le Lay, T. Zecho and J. Kupper, Chem. Phys. Lett. 425 99 (2006)



3-atom clusters

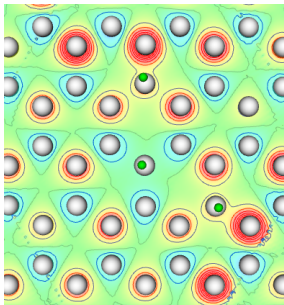
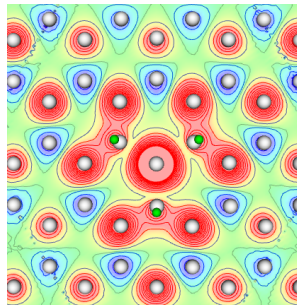


$$\mu = 1\mu_B \Rightarrow \mu = 2\mu_B \Rightarrow \mu = 3\mu_B$$

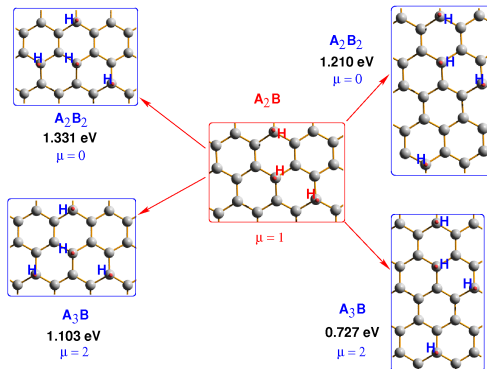


Clustering of H atoms

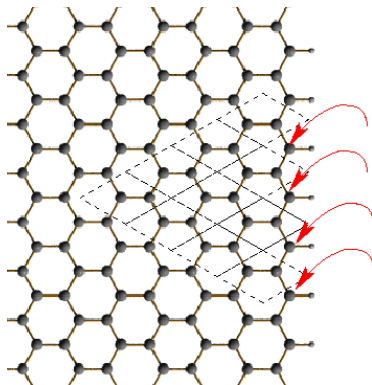
3-atom clusters

 A_2B  A_3 

4-atom clusters



Role of edges

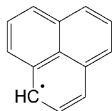


- *zig-zag* edges have enhanced hydrogen affinity
- geometric effects can be investigated in small graphenes

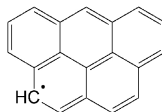
⇒ DFT and **Multi-Reference Quasi-Degenerate PT** on CASSCF wavefunctions

Cluster models to graphene

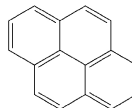
Systems



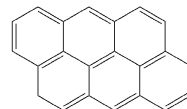
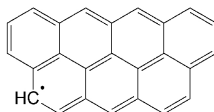
perinaftene / fenalene



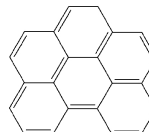
benzo[cd]pirenile



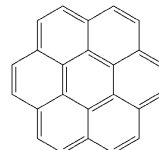
pirene

dibenzo[def,mno]crisene /
antrantrene

7 - PAH



benzo[ghi]perilene



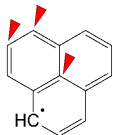
coronene

imbalanced 'PAHs'

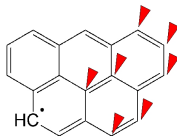
balanced PAHs



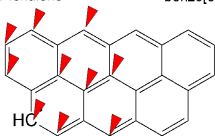
Systems



perinaphthenyl / fenele

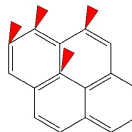


benzo[cd]pirenyle

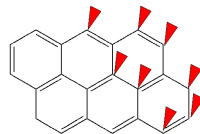
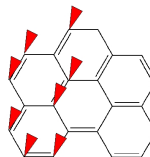


7 - PAH

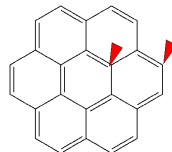
imbalanced 'PAHs'



pirene

dibenzo[def,mno]crisene /
antrantrene

benzo[ghi]perilene



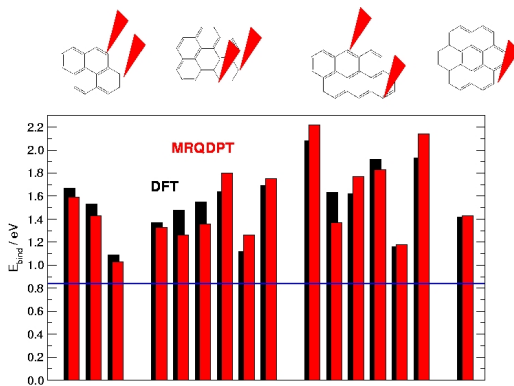
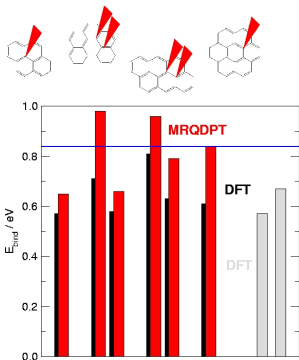
coronene

balanced PAHs

Cluster models to graphene

Balanced PAHs

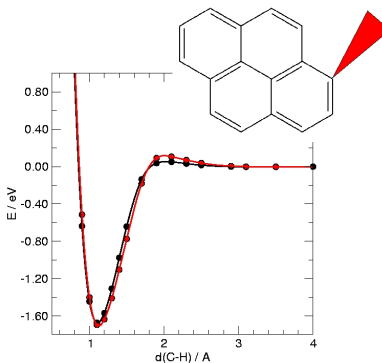
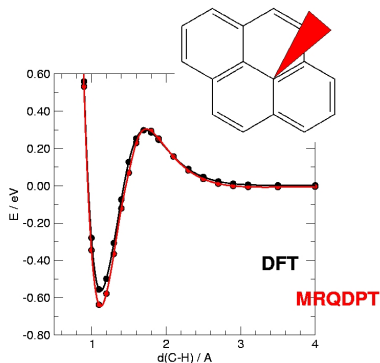
Graphitic vs edge carbons



Cluster models to graphene

Adsorption paths

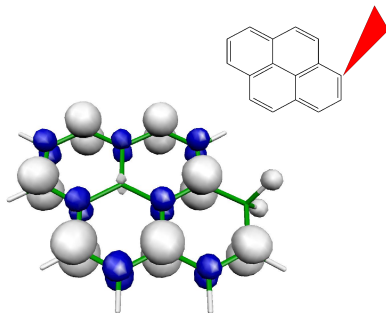
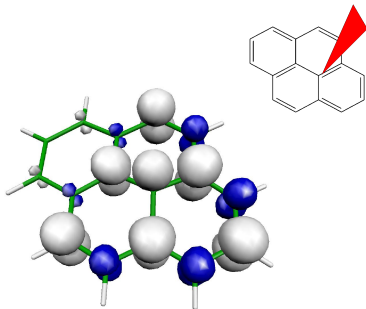
Balanced PAH



Cluster models to graphene

Spin-density

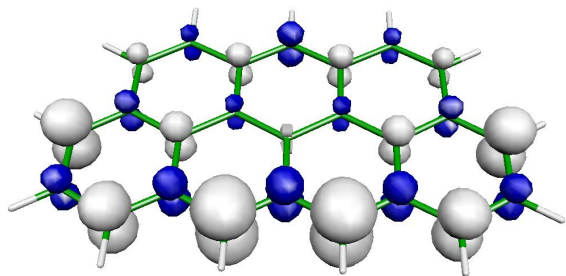
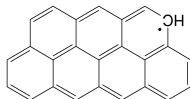
H + Balanced PAH



Cluster models to graphene

Spin-density

Imbalanced PAH



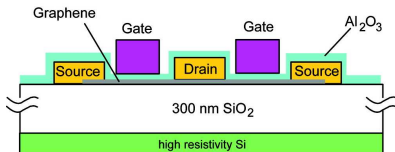
Outline

- 1 Introduction
 - General
 - Basics
- 2 H atoms on graphenic substrates
 - Single atom adsorption
 - Clusters of H atoms
 - The role of edges
- 3 Opening a bandgap
 - H superlattices

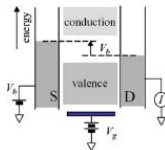


Logic applications

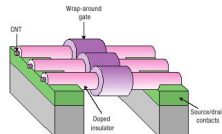
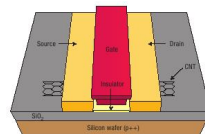
The need for opening a gap



$$n_S = \epsilon_0 \epsilon \frac{V_g}{t e}$$



P. Avouris *et al.*, *Nat. Mat.*, 605, 2, (2007)

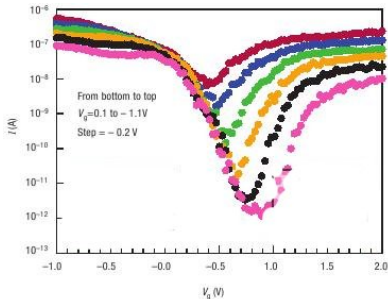


CNT-FET with ordinary and wrapped around gates

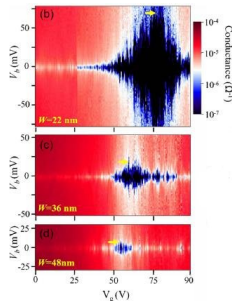


Logic applications

The need for opening a gap



$I - V_g$ characteristics of a CNT-FET



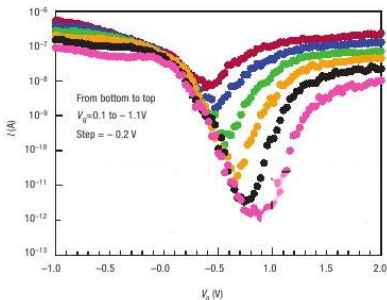
$I = I(V_g, V_{ds})$ for a 20 nm-wide GNR-FET

M. Han *et al.*, *Phys. Rev. Lett.* 98, 206805 (2007)

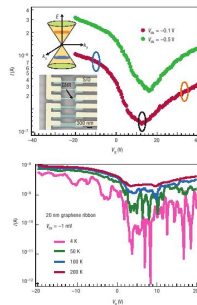


Logic applications

The need for opening a gap



$I - V_g$ characteristics of a CNT-FET



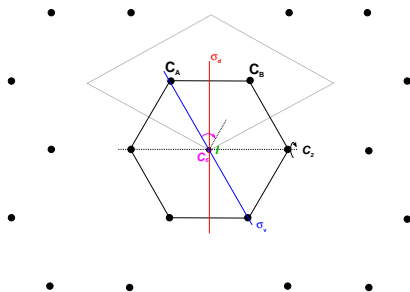
$I = I(V_g, V_{ds})$ GNR-FET



Symmetry

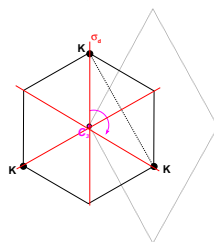
Why graphene is gapless?

r-space



$$G_0 = D_{6h}$$

k-space

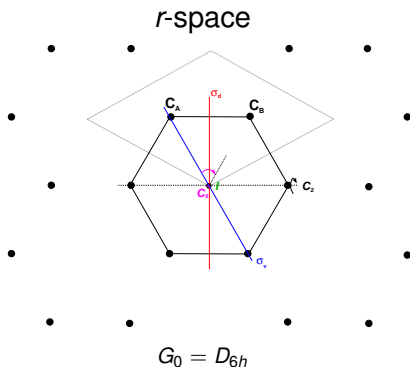


$$G(\mathbf{k}) = \{g \in G_0 | g\mathbf{k} = \mathbf{k} + \mathbf{G}\}$$

$$\Rightarrow G(\mathbf{K}) = D_{3h}$$

Symmetry

Why graphene is gapless?



$$|A_{\mathbf{k}}\rangle = \frac{1}{\sqrt{N_{BK}}} \sum_{\mathbf{R} \in BK} e^{-i\mathbf{k}\mathbf{R}} |A_{\mathbf{R}}\rangle$$

$$|B_{\mathbf{k}}\rangle = \frac{1}{\sqrt{N_{BK}}} \sum_{\mathbf{R} \in BK} e^{-i\mathbf{k}\mathbf{R}} |B_{\mathbf{R}}\rangle$$

$$\langle r | A_{\mathbf{r}} \rangle = \phi_{pZ}(\mathbf{r} - \mathbf{R}_A)$$

for $\mathbf{k} = \mathbf{K}$

$\{|A_{\mathbf{k}}\rangle, |B_{\mathbf{k}}\rangle\}$ span the E'' irrep of D_{3h}



Symmetry and *bipartite* lattices

Theorem

For any bipartite lattice at *half-filling*, if the number of E irreps is *odd* at a special point, there is a degeneracy *at the Fermi level*, i.e. $E_{\text{gap}} = 0$

Proof.

Use electron-hole symmetry

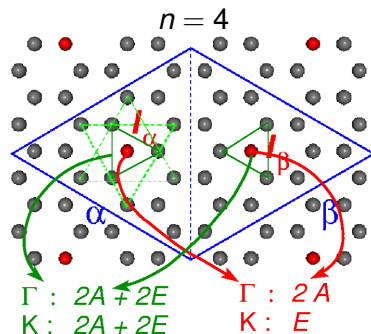


Designing semiconducting structures

- Consider nxn graphene **superlattices** (i.e. $G = D_{6h}$): degeneracy is expected at Γ , K
- Introduce p_z vacancies while **preserving** point symmetry
- Check whether it is possible to turn the **number of E irreps** to be **even both** at Γ **and** at K



Counting the number of E irreps



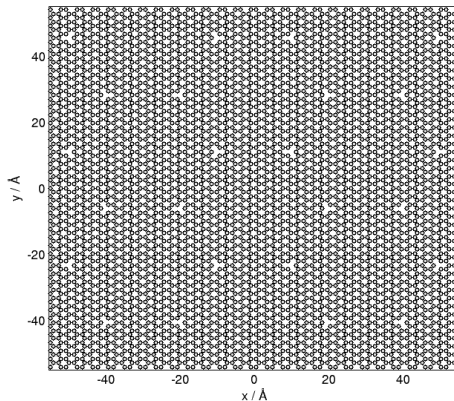
Γ	A	E
$\bar{0}_3$	$2n^2$	$2n^2$
$\bar{1}_3$	$2(3n^2 + 2n + 1)$	$2(3n^2 + 2n)$
$\bar{2}_3$	$2(3n^2 + 4n + 2)$	$2(3n^2 + 4n + 1)$

K_n	A	E
$\bar{0}_3$	$2n^2$	$2n^2$
$\bar{1}_3$	$2n(3n + 2)$	$2n(3n + 2) + 1$
$\bar{2}_3$	$2(3n^2 + 4n + 1)$	$2(3n^2 + 4n + 1) + 1$

$$\Rightarrow n = 3m + 1, 3m + 2, m \in \mathbb{N}$$

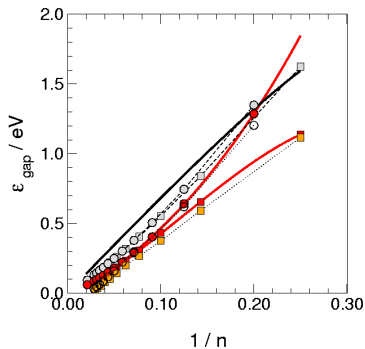


$(14, 0)$ -honeycomb



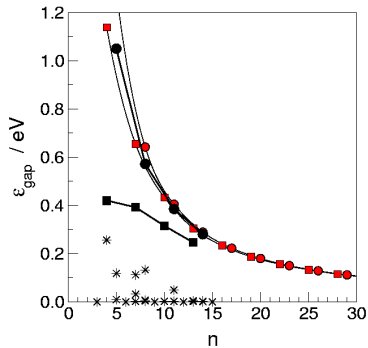
H superlattices

Tight-binding

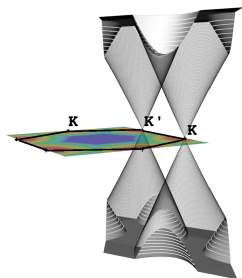


$$\epsilon_{\text{gap}}(K) \sim 2t\sqrt{1.683/n}$$

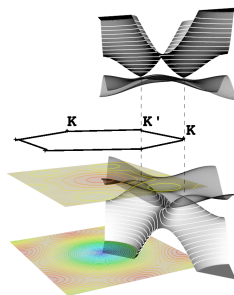
DFT



..not only: as degeneracy may still occur at $\epsilon \neq \epsilon_F$
new Dirac points are expected



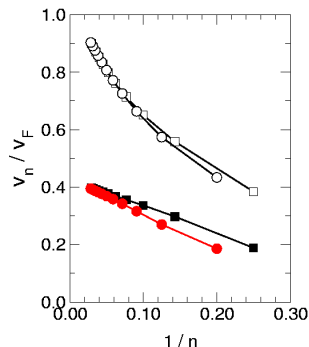
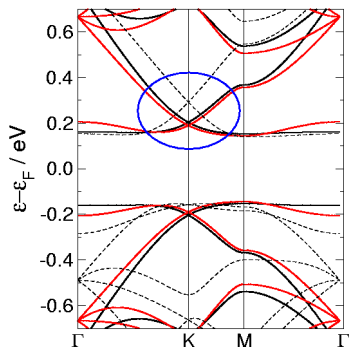
graphene (4x4)



(4,0)-honeycomb



..not only: as degeneracy may still occur at $\epsilon \neq \epsilon_F$
new Dirac points are expected



Summary

- Thermodynamically and kinetically favoured H clusters **minimize** sublattice imbalance
- Adsorption on magnetic C-substrates is roughly governed by **spin density** only
- Symmetry *breaking* is **not** necessary to open a gap
- New Dirac cones appears right **close** to the edges of the gap region



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Center

Notur

I.S.T.M.



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Thank you for your attention!